

# Measurement of $V_{us}$ . Recent NA48 results on semileptonic and rare Kaon decays

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# Introduction

- CKM Unitarity
- NA48 Experimental setup
- Measurement of  $\text{Br}(K^0_L e^3)/\text{Br}(2\pi)$
- $\text{Br}(K^0_L e^3)$
- Measurement of  $\text{Br}(K^0_L \rightarrow 3\pi^0)$
- Measurement of  $\text{Br}(K^\pm e^3)$
- Extraction of  $V_{us}$
- $K^0_L e^3$  form factors
- Radiative decay  $\text{Br}(K^0_L e^3 \gamma)$
- Rare decays
  - $K^0_L \rightarrow e^+ e^- \gamma$  form factor
  - $\text{Br}(K^0_L \rightarrow e^+ e^- e^+ e^-)$
  - $K^0_{e4}$  decay
  - Search for  $K^0_s \rightarrow 3\pi^0$
  - Observation of  $K^0_s \rightarrow \pi^0 \mu^+ \mu^-$
- Conclusions

# CKM Unitarity

Unitarity of CKM matrix requires for the first row

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$

PDG 2004 data

$$|V_{ud}| = 0.9738 \pm 0.0005 \quad \text{- well measured}$$

$$|V_{ub}| = (3.67 \pm 0.47) \cdot 10^{-3} \quad \text{- ( } |V_{ub}|^2 \approx 10^{-5} \text{ negligible)}$$

SM prediction

$$|V_{us}| = 0.2274 \pm 0.0021$$

Experimental value

$$|V_{us}| = 0.2200 \pm 0.0026$$

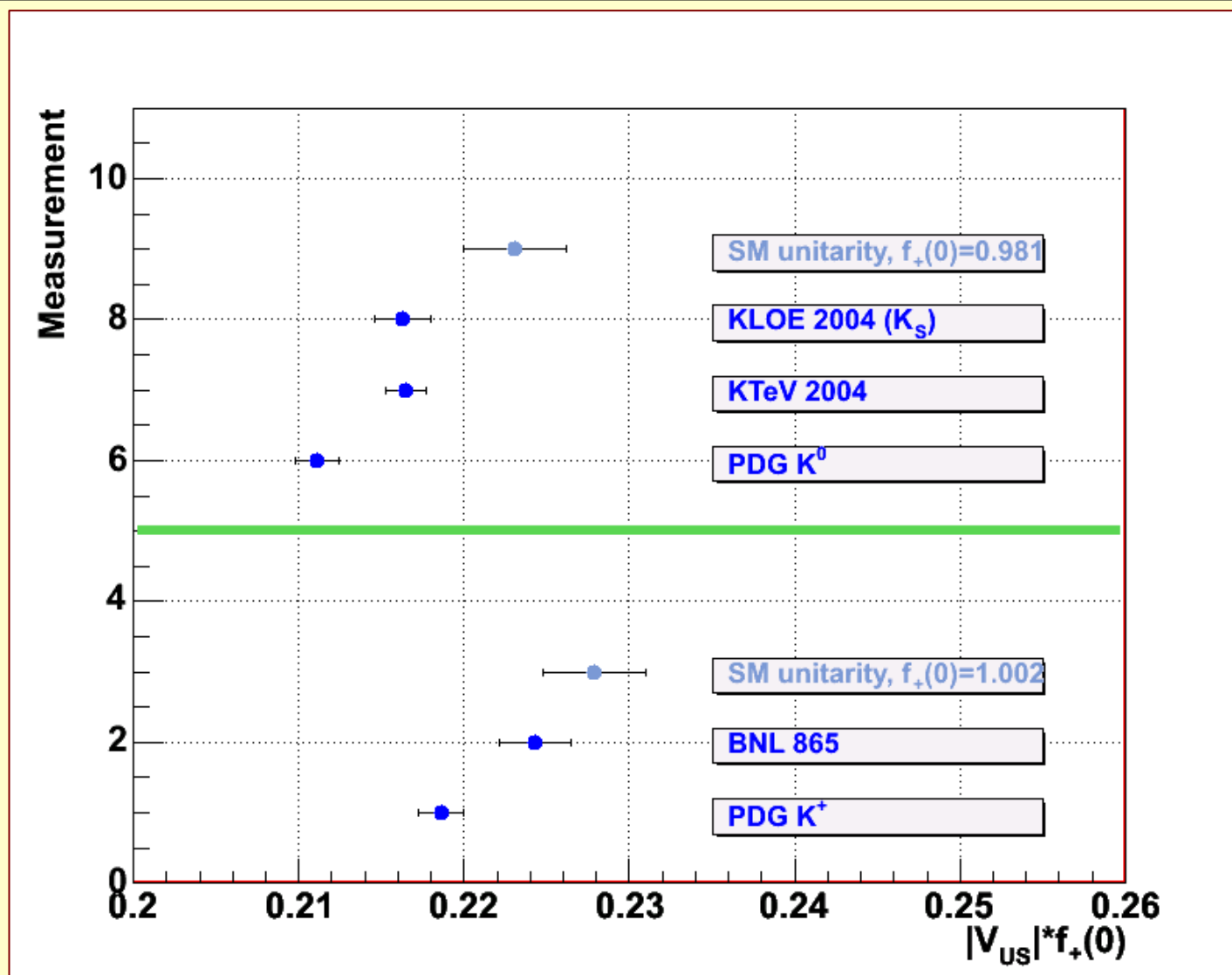
$$\Delta|V_{us}| = 0.0074 \pm 0.0033 \quad \sim 2.2 \sigma \text{ discrepancy}$$

To solve the problem – measurement with precision  $\sim 1\%$  (limited by theory)

Semileptonic decays  $K \rightarrow \pi e \nu$  best for determination of  $|V_{us}|$

Recent measurements from  $K^+ e3$  (BNL2003) and  $K^0 e3$  (KTeV) and KLOE,prel, 2004) are significantly above previous results.

$$V_{us}f_+(0)$$



# NA48 experiment

## □ Main detector components

### ❖ Magnet spectrometer

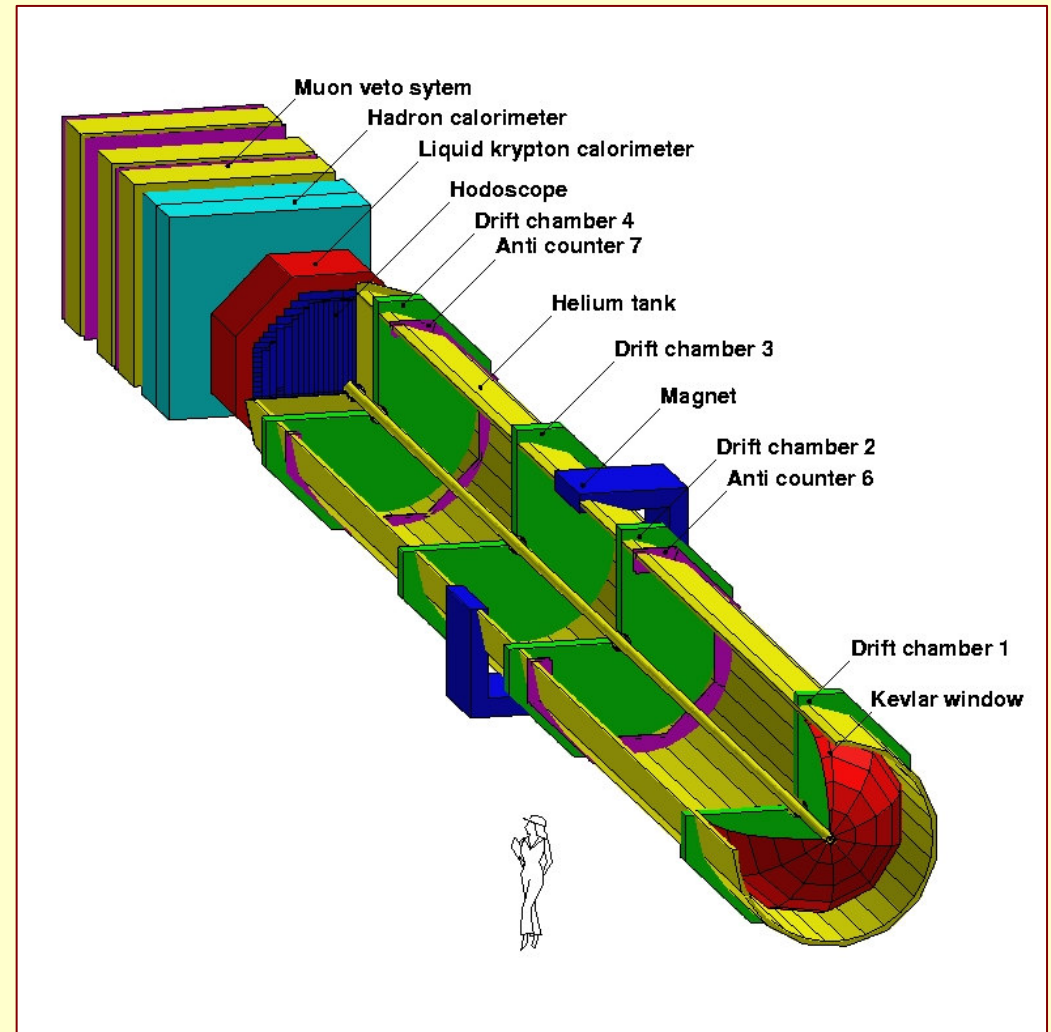
- Two drift chambers before and two after spectrometer magnet
- Momentum resolution  $< 1\%$  for 20 GeV/c momentum

$$\frac{\delta E}{E} = \frac{3.2\%}{\sqrt{E[\text{GeV}]}} \oplus \frac{90\text{MeV}}{E} \oplus 0.42\%$$

### ❖ Hadron Calorimeter

### ❖ Muon Veto system

### ❖ Beams – $K_L^0, K_S^0, K^\pm$



## New NA48 results

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Vus measurement

## $K_L^0 \rightarrow \pi e \nu$

### ❖ Semileptonic $K_L$ decays $K_L^0 \rightarrow \pi l \nu$

- Data from special minimum bias run 1999 with pure  $K_L^0$  beam
- Very high statistics available – 80 million triggers taken

### ❖ General idea

- Normalize to as many as possible channels
- Data selection and analysis - as simple as possible

### ❖ Measure the ratio $\text{Br}(K_L^0 \rightarrow e3)/\text{Br}(2\text{tr})$    $2\text{tr} =$ all $K_L^0$ decays with two charged particles in the spectrometer

- Normalization on

$$\text{Br}(2\text{tr}) = 1.0048 - \text{Br}(K_L^0 \rightarrow 3\pi^0)$$

$$K_L^0 \rightarrow \pi e \nu$$

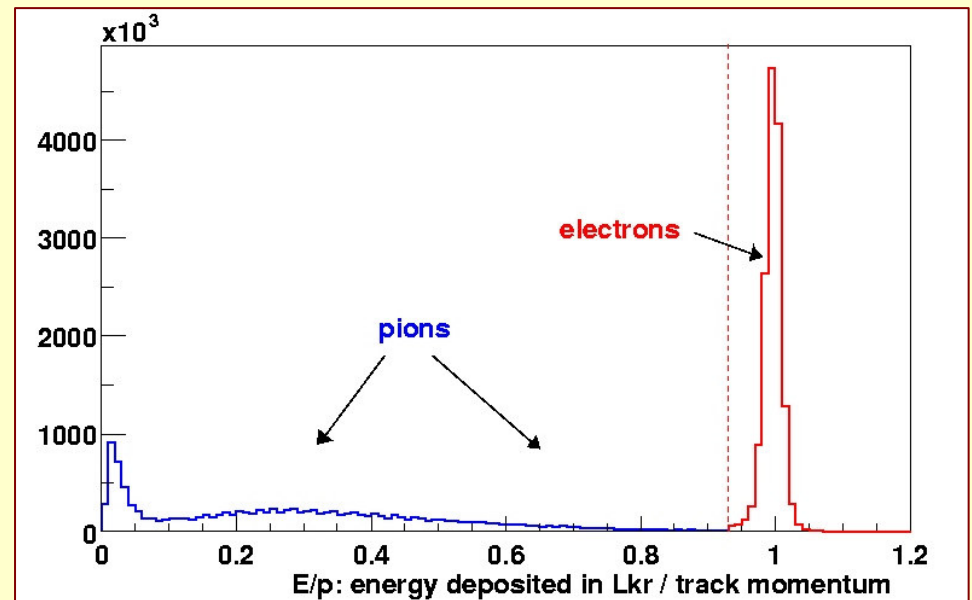
❖ Main selection criteria for 2 track sample

- Decay vertex within 8 m and 33 m from final collimator
- Track separation in LKr > 25 cm
- Track momenta > 10 GeV
- $P_{\text{sum}} = P_1 + P_2 > 60 \text{ GeV}$

12.6 million 2 track events

❖  $K_L^0 \rightarrow \pi e \nu$  selection – the same but

- $E(\text{LKr})/p > 0.93$



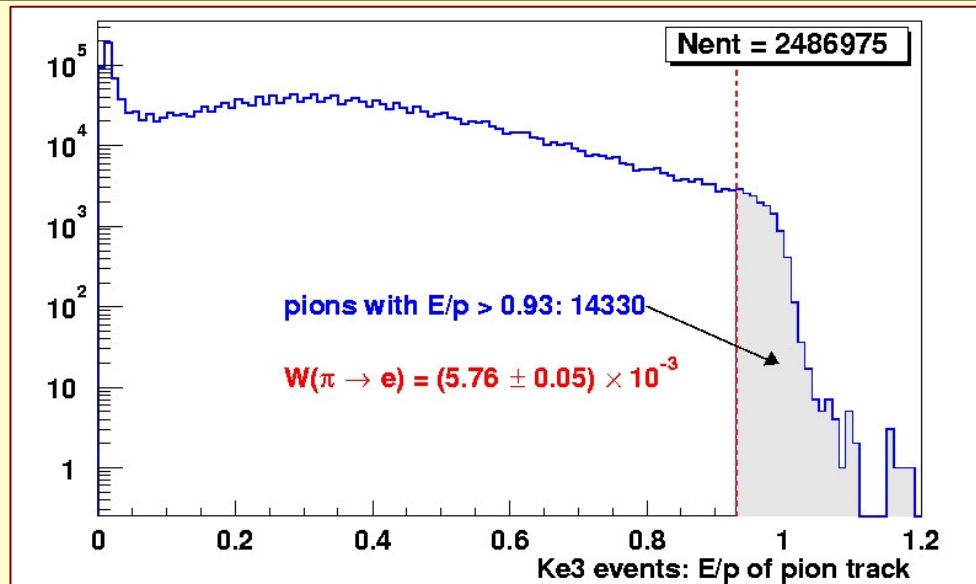


# $K_L^0 \rightarrow \pi e \nu$

## ❖ Background to $K_{e3}$ sample

- BG from  $K\mu 3$  and  $K3\pi$  with  $\pi^\pm$  misidentified as  $e^\pm$
- Estimate the BG from  $K_{e3}$  data with identified  $e^\pm$  ( $E/p > 1$ )

$$P(\pi \rightarrow e) = 5.8 \cdot 10^{-3}$$

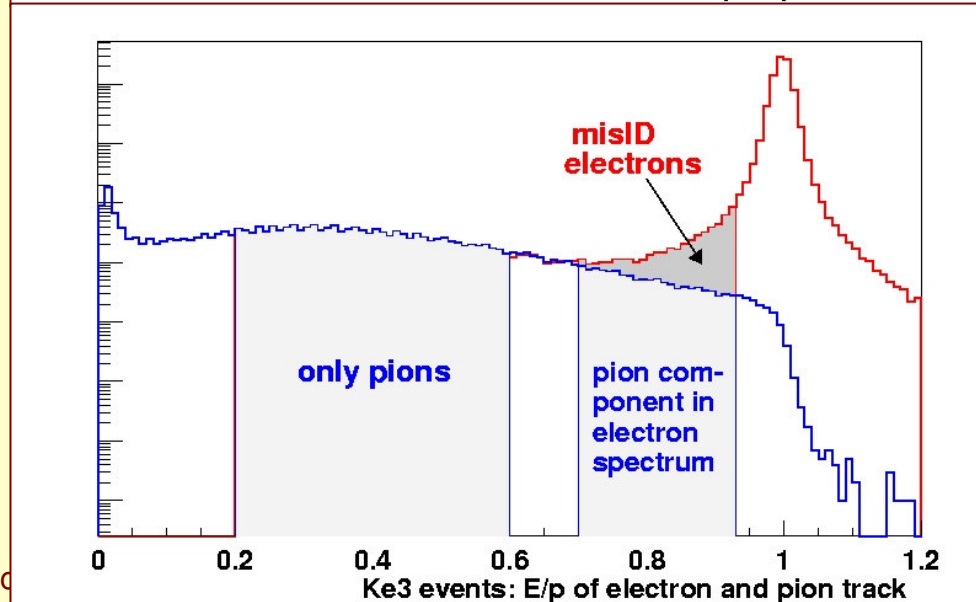


## ❖ Inefficiency of electron ID

- Estimate  $e^\pm$  inefficiency from  $K_{e3}$  data with identified  $\pi^\pm$  ( $0.3 < E/p < 0.7$ )

$$P(e \rightarrow \pi) = 4.9 \cdot 10^{-3}$$

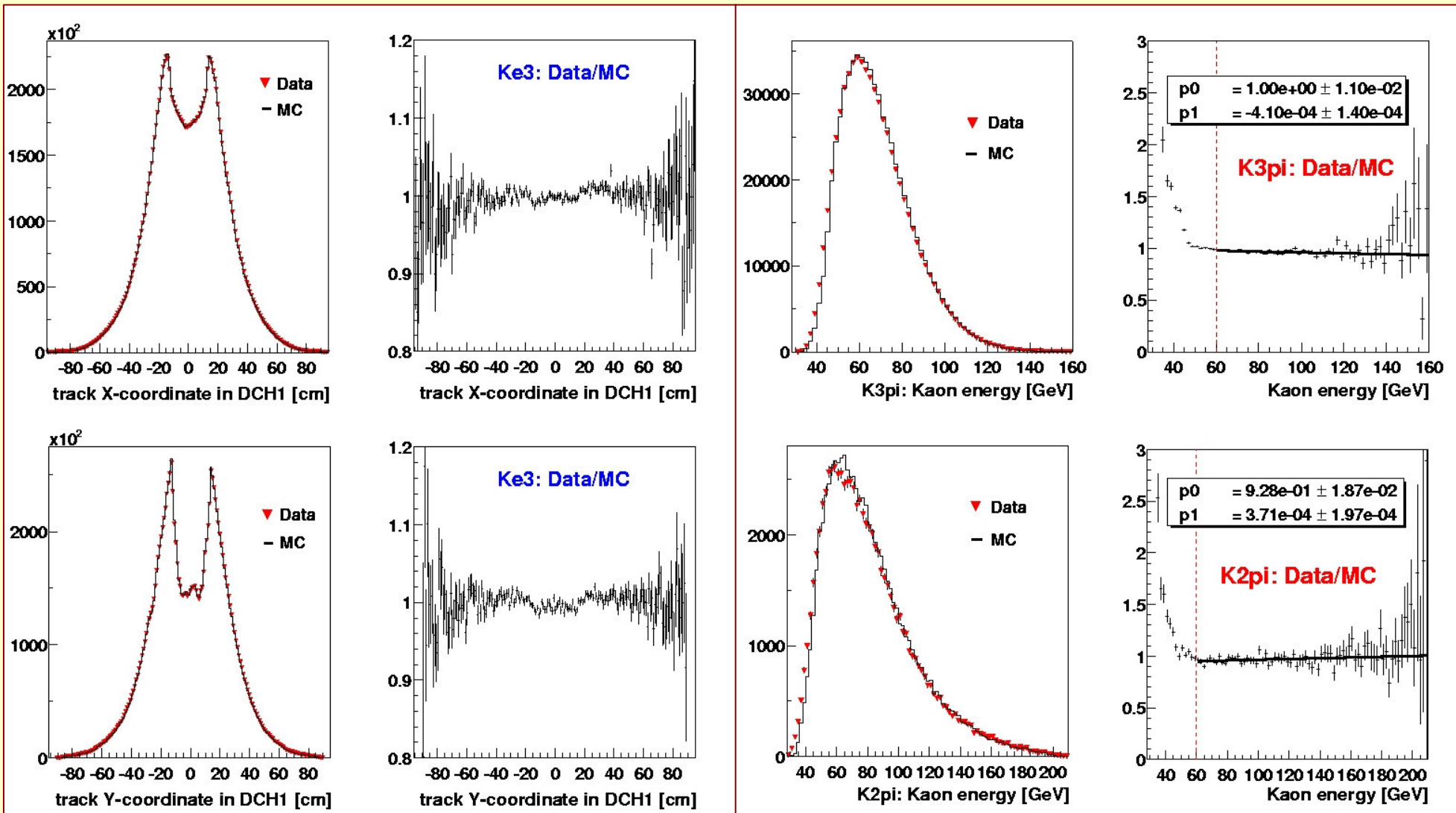
Selected 6.7 million  $K_{e3}$



## $K^0_L \rightarrow \pi e \nu$

- ❖ Monte Carlo simulation of detector acceptance
  - All two track channels involved – (Ke3, Kμ3, K3π, K2π, K3π<sub>D</sub>)
  - For average 2-track acceptance use Br fractions
  - Average from PDG and KTeV (Bμ3/Be3, B3π/Be3,....)
$$A_{2tr} = 0.2412 \pm 0.0004$$
- ❖ Ke3 simulation includes radiative corrections and Ke3γ with real photons  
Ginsberg (Phys.Rev. 171, 1675(1968)+ errata)
- ❖ Good agreement between MC and data except for high momentum  $K^0_L$
- ❖ Systematic errors
  - Main contribution comes from inexact knowledge of beam momentum  
(can be reconstructed only up to quadratic ambiguity)
  - For measurement of beam momentum distribution – K2pi and K3pi decays
  - Experimental uncertainty of 0.7% on measured ratio
- ❖ Statistical errors are negligible

# $K_L^0 \rightarrow \pi e \nu$



$$K^0_L \rightarrow \pi e \nu$$

## Experimental result

$$\text{Br}(K^0_L e3)/\text{Br}(2\text{tr}) = 0.498 \pm 0.004$$

Preliminary

To determine  $\text{Br}(K^0_L \rightarrow \pi e \nu)$  we need  $\text{Br}(K^0_L \rightarrow 3\pi^0)$

PDG04:  $\text{Br}(K^0_L \rightarrow 3\pi^0) = 0.2105 \pm 0.0028$

KTeV  $\text{Br}(K^0_L \rightarrow 3\pi^0) = 0.1945 \pm 0.0018$  ?

Average according PDG prescription

$$\text{Br}(K^0_L \rightarrow 3\pi^0) = 0.1992 \pm 0.0070$$

$$\text{Br}(K^0_L e3) = 0.4010 \pm 0.0028_{\text{exp}} \pm 0.0035_{\text{norm}}$$

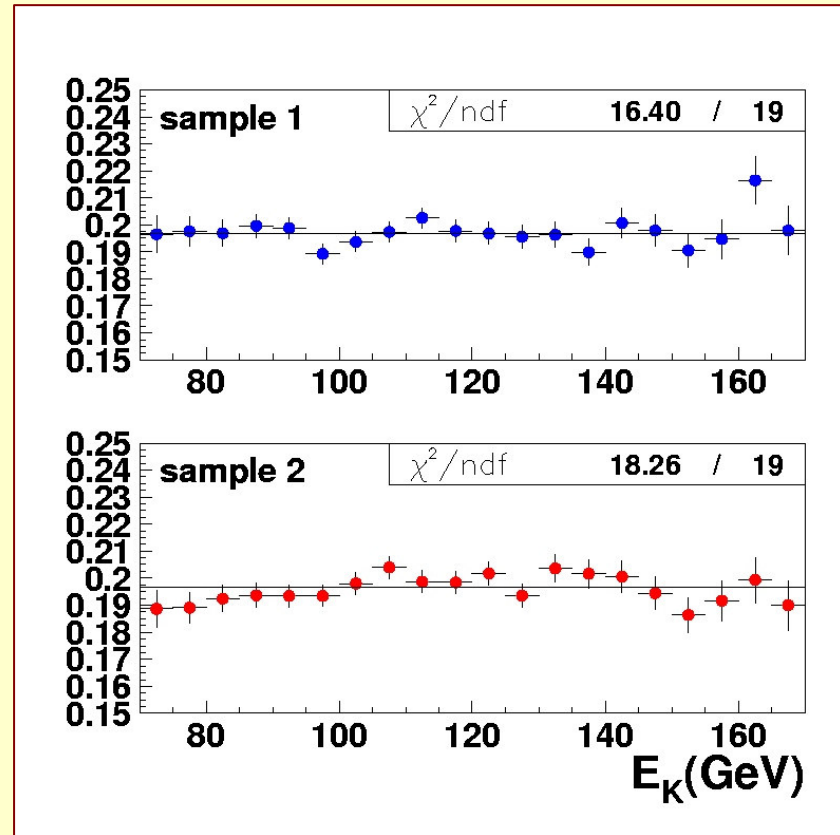
Preliminary

## Measurement of $\text{Br}(K_L^0 \rightarrow 3\pi^0)$

- ❖  $\text{Br}(K_L^0 \rightarrow 3\pi^0)$  is the main experimental uncertainty on  $\text{Br}(K_L^0 \rightarrow e^+e^-3\pi^0)$ 
  - PDG (Kreutz et al 1995) inconsistent with new KTeV result by  $\approx 5 \sigma$
  - Measure  $\text{Br}(K_L \rightarrow \pi^0\pi^0\pi^0) / \text{Br}(K_S \rightarrow \pi^0\pi^0)$
  - $\text{Br}(K_S \rightarrow \pi^0\pi^0) = 0.3104 \pm 0.0014$  well measured
- ❖ NA48/1 data, 2000:
  - High intensity  $K_S$  beam
  - No material (DCH etc) between collimator and LKr calorimeter
  - Ideal for measurement of neutral Kaon decays
- ❖ We used only small amount of 2000 data
  - $\sim 200\,000 K_L \rightarrow \pi^0\pi^0\pi^0$
  - $\sim 600\,000 K_S \rightarrow \pi^0\pi^0$
  - Two independent samples
  - Same number of  $K_L$  and  $K_S$  is produced on the target

## Measurement of $\text{Br}(K_L^0 \rightarrow 3\pi^0)$

- ❖ Main systematic
- LKr energy scale  $\pm 0.0020$
- Effective target position  $\pm 0.0017$
- $K_L$  life time:  $\pm 0.0015$



$$\text{Br}(K_L \rightarrow \pi^0\pi^0\pi^0) = 0.1966 \pm 0.0006_{\text{stat}} \pm 0.0033_{\text{syst}}$$

Preliminary

In a good agreement with KTeV result

## Measurement of $\text{Br}(K^\pm \rightarrow \pi^0 e^\pm \nu)$

- ❖ NA48/2 data from 2003

- Low intensity  $K^+/K^-$  run (8 hours) with minimum bias trigger

- ❖ Normalize  $K^\pm \rightarrow \pi^0 e^\pm \nu$  decays to  $K^\pm \rightarrow \pi^\pm \pi^0$

$$\text{Br}(K^\pm \rightarrow \pi^\pm \pi^0) = 0.2113 \pm 0.0014$$

- ❖ Selected events

$$K^+ \rightarrow \pi^0 e^+ \nu \quad 59\,000 \text{ ev.}$$

$$K^- \rightarrow \pi^0 e^- \nu \quad 33\,000 \text{ ev.}$$

$$K^+ \rightarrow \pi^+ \pi^0 \quad 468\,000 \text{ ev.}$$

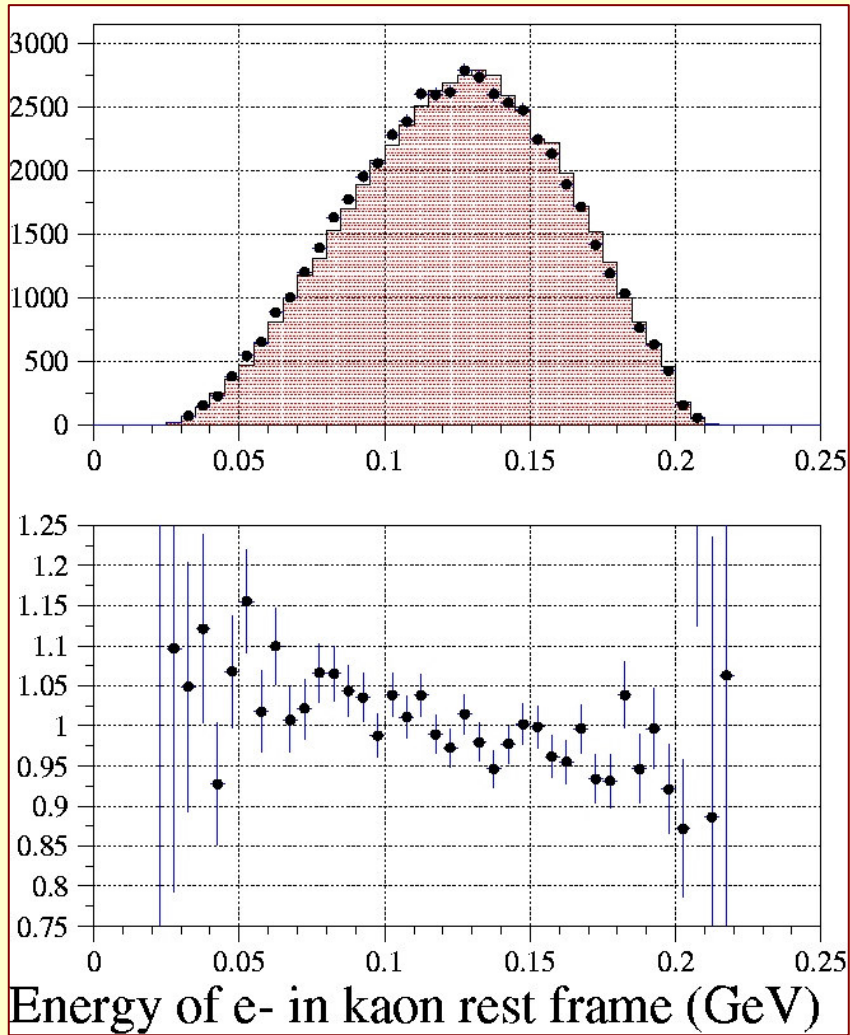
$$K^- \rightarrow \pi^- \pi^0 \quad 260\,000 \text{ ev.}$$

- ❖ Practically background free

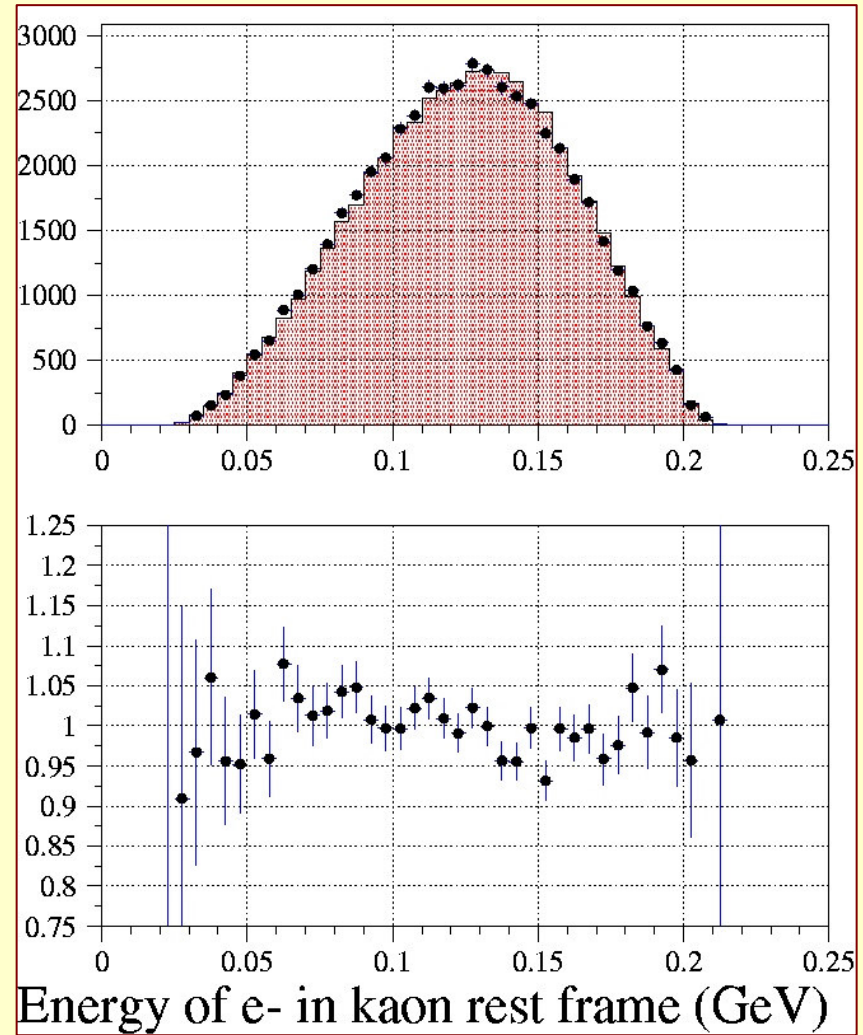
- ❖ Systematic

- Main sources – Detector acceptance,  $\text{Br}(K^\pm \rightarrow \pi^\pm \pi^0)$ , MC statistic

# Measurement of $\text{Br}(K^\pm \rightarrow \pi^\pm e\nu)$



Without radiative corrections



With radiative corrections



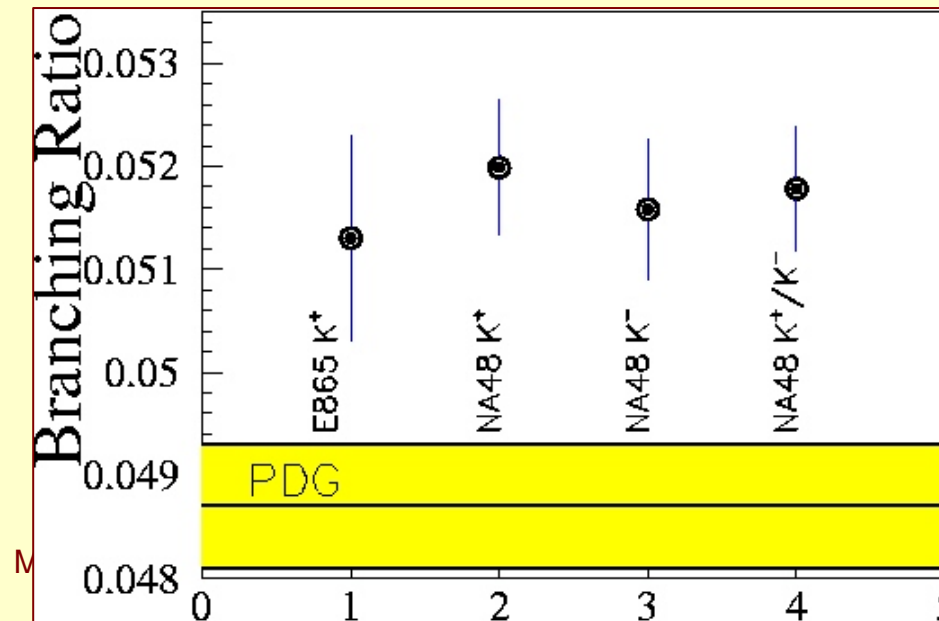
# Measurement of $\text{Br}(K^\pm \rightarrow \pi^0 e^\pm \nu)$

Preliminary NA48/2 result on  $\text{Br}(K^\pm \rightarrow \pi^0 e^\pm \nu)$

$$\text{Br}(K^+ \rightarrow \pi^0 e^+ \nu) = (5.163 \pm 0.021_{\text{stat}} \pm 0.056_{\text{syst}}) \%$$

$$\text{Br}(K^- \rightarrow \pi^0 e^- \nu) = (5.093 \pm 0.028_{\text{stat}} \pm 0.056_{\text{syst}}) \%$$

$$\text{Br}(K^\pm \rightarrow \pi^0 e^\pm \nu) = (5.14 \pm 0.02_{\text{stat}} \pm 0.06_{\text{syst}}) \%$$



## Determination of $V_{us}$

$|V_{us}|$  can be extracted from  $K \rightarrow \pi e \nu$  via

$$|V_{us}| \cdot f_+^{K\pi}(0) = \sqrt{\frac{128 \pi^3 \Gamma(Ke3(\gamma))}{C^2 G_F^2 M_K^5 S_{EW} I_K}}$$

Where:

$S_{EW} = 1.0232$  – short distance enhancement factor,

$I_K$  - phase space integral,

$$C = \begin{cases} 1 & K_{e3}^0 \\ 1/\sqrt{2} & K_{e3}^+ \end{cases}$$

$$f_+^{K^0\pi^+}(0) = 0.981 \pm 0.010$$

$$f_+^{K^+\pi^0}(0) = 1.002 \pm 0.010$$

We used the values obtained by  
 Cirigliano, Neufeld, Pichl (EPJ C35, 53, 2004)  
 Isospin violation effects, e.m. corrections,  
 $O(p^6)$  terms are taken into account

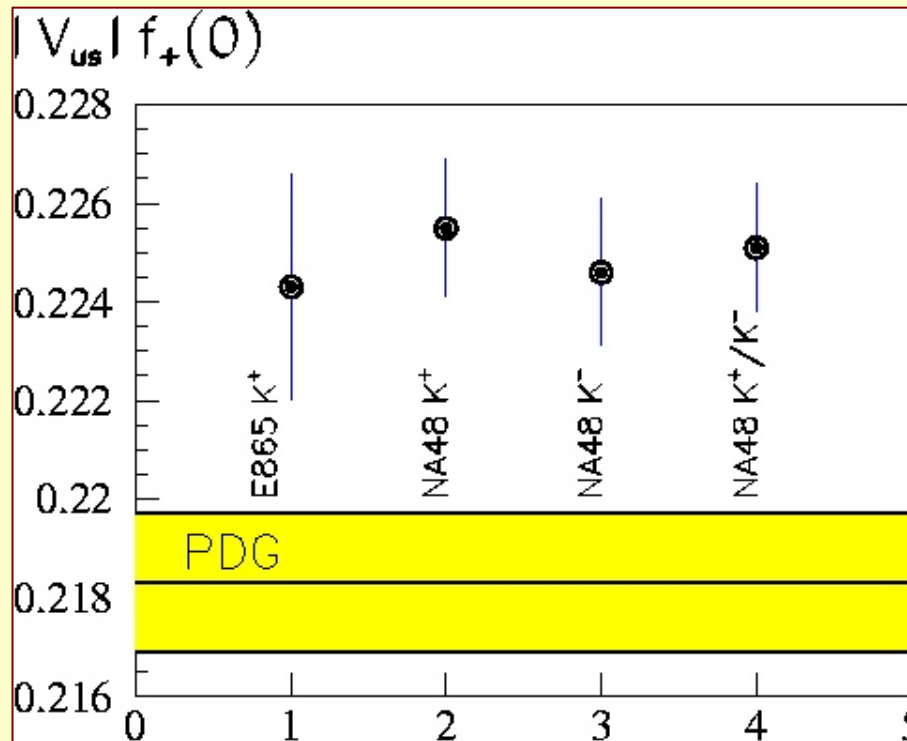
## Determination of $V_{us} f_+(0)$

$$|V_{us}| \cdot f_+^{K^0 \pi^+}(0) = 0.2146 \pm 0.0016$$

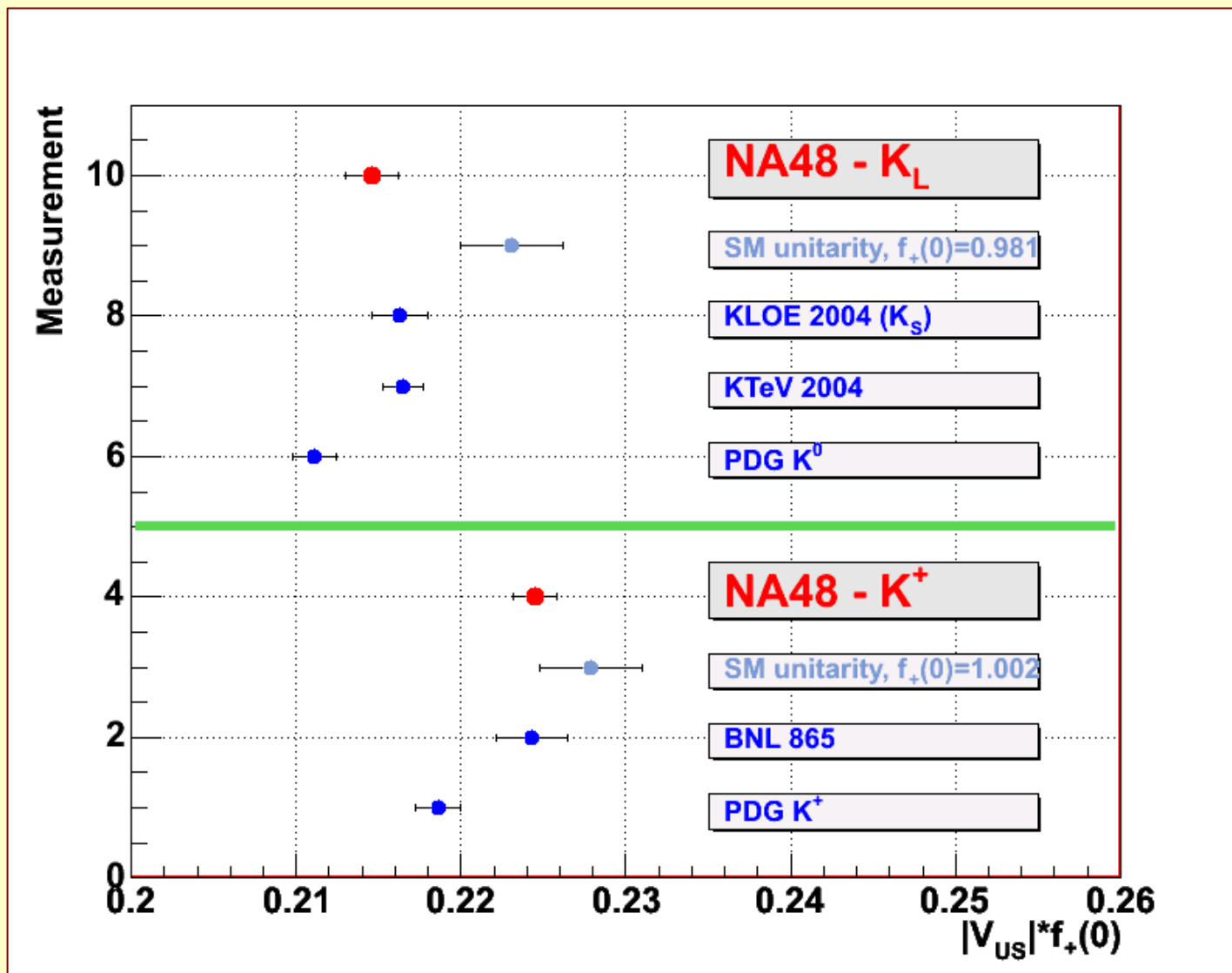
$$|V_{us}| \cdot f_+^{K^+ \pi^0}(0) = 0.2250 \pm 0.0013$$

$$|V_{us}| \cdot f_+^{K^- \pi^0}(0) = 0.2235 \pm 0.0014$$

$$|V_{us}| \cdot f_+^{K^\pm \pi^0}(0) = 0.2245 \pm 0.0013$$



# Determination of $V_{us}f_+(0)$



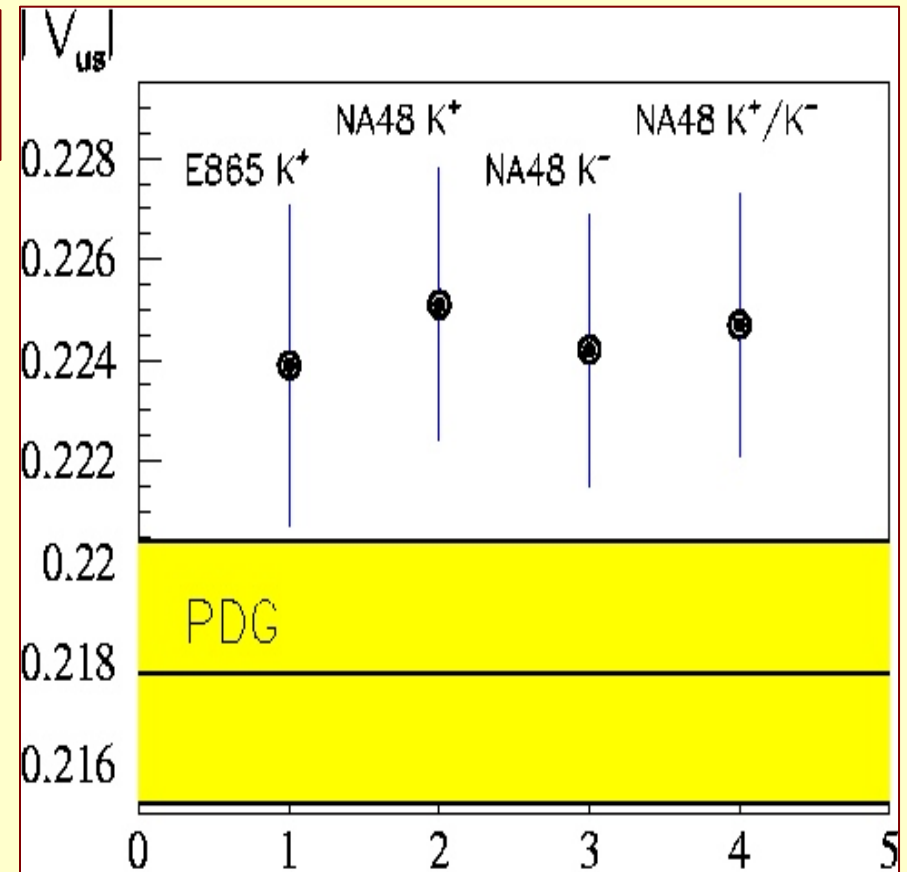
## Determination of $V_{us}$

$$|V_{us}|^{K^0\pi^+}(0) = 0.2187 \pm 0.0016_{\text{exp}} \pm 0.0023_{\text{theor}}$$

$$|V_{us}|^{K^+\pi^0}(0) = 0.2246 \pm 0.0013_{\text{exp}} \pm 0.0023_{\text{theor}}$$

$$|V_{us}|^{K^-\pi^0}(0) = 0.2231 \pm 0.0014_{\text{exp}} \pm 0.0023_{\text{theor}}$$

$$|V_{us}|^{K^\pm\pi^0}(0) = 0.2241 \pm 0.0013_{\text{exp}} \pm 0.0023_{\text{theor}}$$



# Determination of $V_{us}$

## Conclusions

### Experimental determination of $V_{us}$ from

- ❖  $K^\pm$ 
  - in disagreement with old measurements (PDG)
  - in agreement with BNL result and SM prediction
- ❖  $K_L^0$ 
  - in disagreement with old measurements (PDG)
  - In agreement with new KTeV and KLOE measurements
  - Still in disagreement with SM prediction  $\sim 2.5 \sigma$
- ❖ Main uncertainty comes from theoretical calculations of  $f_+(0)$ 
  - More accurate calculation of  $O(p6)$  contribution required

## New NA48 results

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## Other results

# Ke3 form factors

❖  $K_L \rightarrow \pi e \nu$  form factors the same 1999 data

- 5.6 million reconstructed events
- Preliminary result for pure vector interaction

$$\lambda_+ = 0.0288 \pm 0.0005_{\text{stat}} \pm 0.0011_{\text{syst}}$$

➤ Preliminary result for 3-parameter fit:

$$\lambda_+ = 0.0284 \pm 0.0007 \pm 0.0013$$

$$\left| \frac{f_S}{f_+(0)} \right| = 0.015^{+0.007}_{-0.010} \pm 0.0012$$

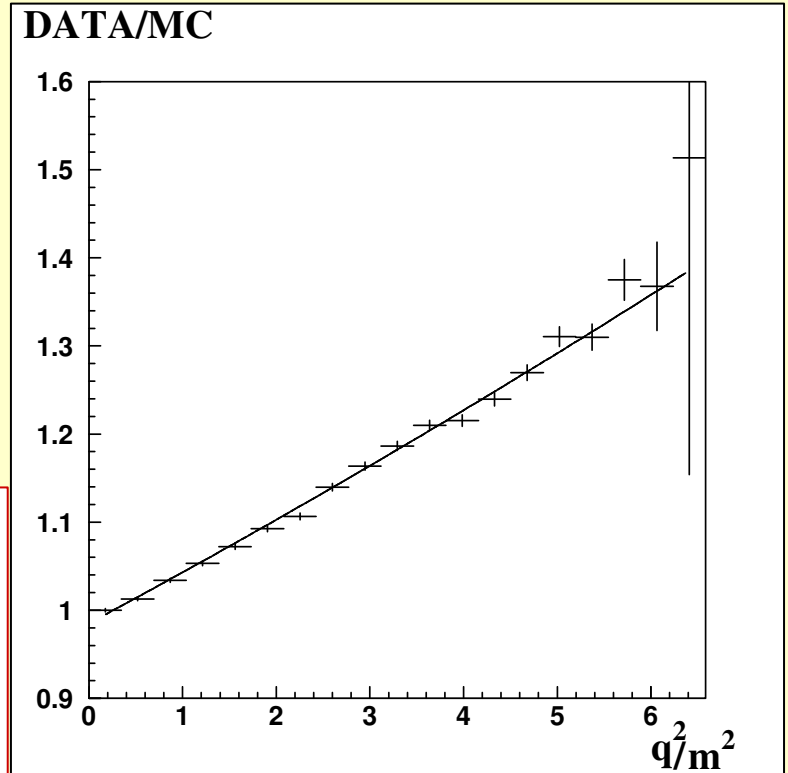
$$\left| \frac{f_T}{f_+(0)} \right| = 0.05^{+0.03}_{-0.04} \pm 0.03$$

PDG(2004):

$$\lambda_+ = 0.0291 \pm 0.0018$$

$$\left| \frac{f_S}{f_+(0)} \right| < 0.04$$

$$\left| \frac{f_T}{f_+(0)} \right| < 0.23$$



❖ No evidence for scalar and tensor couplings!



# $K^0_L \rightarrow \pi e \nu \gamma$

## ❖ Data analysis

➤ Tight selection in order to suppress background from

$K_{3\pi}$ ,  $K_{e4}$  and

$K_{e3} + \text{accidental photon}$

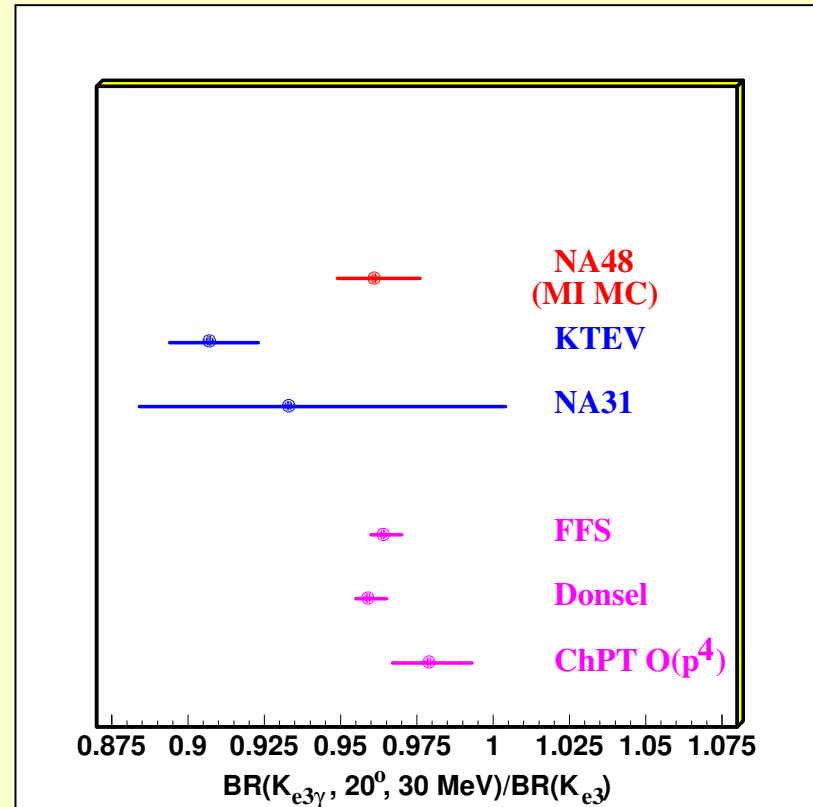
➤ Selected events:

19000 :  $K_{e3\gamma}$

5.6 million :  $K_{e3}$

0.9  
0.8  
0.5  
0.4  
0.3  
0.2  
0.1  
0

Preliminary result:



$$\frac{\Gamma(K_{e3\gamma}, E_\gamma^* > 30 \text{ MeV}, \theta_{e\gamma}^* > 20^\circ)}{\Gamma(K_{e3})} = (0.964 \pm 0.008^{+0.012}_{-0.011})\%$$

❖ Good agreement with theory predictions!

Measurement of  $V_{us}$ . Recent NA48 results on semileptonic and rare Kaon decays

## Rare decays

□  $K_L^0 \rightarrow e^+e^-\gamma$  form factor

Measures structure of  $\gamma^*$  vertex

NA48 98-2001 data  $\sim 60\,000$  ev.

Preliminary result for BMS form factor

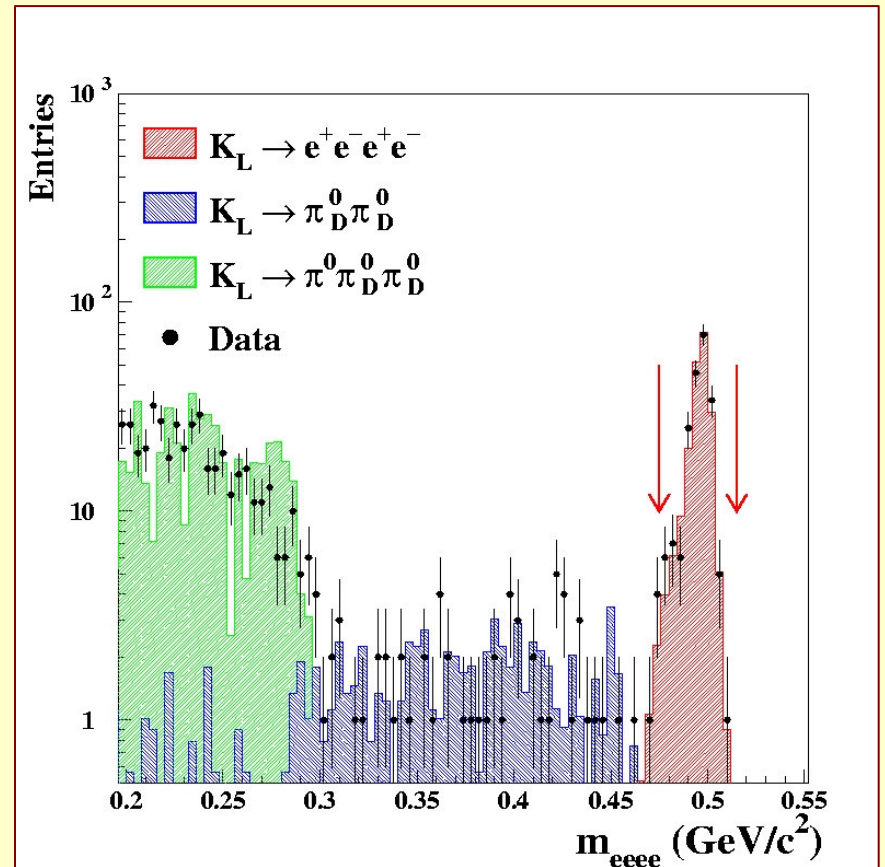
$$\alpha_K^* = -0.207 \pm 0.019 \pm 0.017$$

In good agreement with KTeV

□  $\text{Br}(K_L^0 \rightarrow e^+e^- e^+e^-)$

200 events from 98/99 data

$$\text{Br}(K^\pm \rightarrow e^+e^- e^+e^-) = (3.30 \pm 0.24_{\text{stat}} \pm 0.14_{\text{syst}} \pm 0.24_{\text{norm}}) \times 10^{-8}$$



## Rare decays

### □ $K^0 e 4$ decay

$$\text{Br}(K_L \rightarrow \pi^\pm \pi^0 e^\pm \nu) = (5.21 \pm 0.07_{\text{stat}} \pm 0.09_{\text{syst}}) \times 10^{-5}$$

Precise measurement of the form factors [Phys.Lett B 595,75,2004](#)

### □ Search for $K_s \rightarrow \pi^0 \pi^0 \pi^0$ . Final result on CPV parameter $\eta^{000}$

$$\begin{aligned} \text{Re}(\eta^{000}) &= -0.002 \pm 0.011_{\text{stat}} \pm 0.015_{\text{syst}} \\ \text{Im}(\eta^{000}) &= -0.003 \pm 0.013_{\text{stat}} \pm 0.017_{\text{syst}} \end{aligned}$$

[hep-ex/0408053](#)

$$\text{Br}(K_s \rightarrow \pi^0 \pi^0 \pi^0) < 7.4 \times 10^{-7} \quad 90\% \text{ CL}$$

### □ Observation of 6 $K_s \rightarrow \pi^+ \mu^+ \mu^-$ events

$$\text{Br}(K_s \rightarrow \pi^+ \mu^+ \mu^-) = (2.8 + 0.15_{\text{stat}} - 0.12_{\text{stat}} \pm 0.2_{\text{syst}}) \times 10^{-9}$$

## Conclusions

- ❖ PDG values on  $|V_{us}|$  are in poor agreement with unitarity of the CKM matrix
- ❖ NA48 has performed  $|V_{us}|$  measurements in  $K_L^0 e3$  and  $K^\pm e3$  decays
- ❖  $K_L$  and  $K^\pm$  results are
  - in disagreement with previous PDG values
  - In good agreement with recent results from KTeV and BNL
  - In fair agreement with SM predictions (better for  $K^\pm$ , worse for  $K_L$ )
- ❖ More precise values for  $f_+(0)$  are needed to solve the unitarity dilemma
- ❖ Semileptonic  $K_L$  decays
  - $K_L^0 \rightarrow \pi e \nu$  form factors
  - Radiative decays  $K_L^0 \rightarrow \pi e \nu \gamma$
- ❖  $K_L \rightarrow \gamma^* \gamma^{(*)}$  decays
  - $K_L^0 \rightarrow e^+ e^- \gamma$  form factor and  $K_L^0 \rightarrow e^+ e^- e^+ e^-$
- ❖ Rare  $K_s$  decays
  - First observation of  $K_s \rightarrow \pi^+ \mu^+ \mu^-$
  - Search for  $K_s \rightarrow \pi^0 \pi^0 \pi^0$