Precise measurement of V_{us}

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Introduction

- > CKM unitarity
- Extraction of V_{us}
 - Experimental data
 - Theoretical input
 - Results
 - Compatibility of K⁰ and K^{+/-} results
- Conclusions

Introduction

CKM - Unitarity

CKM Unitarity

```
Unitarity of CKM matrix leads to a number of relations between V<sub>ii</sub>
In particular for the first row
                 |Vud|^2 + |Vus|^2 + |Vub|^2 = 1
Most precisely measured elements of CKM
PDG 2004 data
|Vud| - well determined from measurement of
                 super allowed nuclear \beta-decays
                 free neutron life time
                 |Vud| = 0.9738 \pm 0.0005
                 |Vub| = (3.67 ± 0.47).10<sup>-3</sup> - ( |Vub|<sup>2</sup> ≈ 10<sup>-5</sup> negligible)
SM prediction
                 |Vus| = 0.2274 \pm 0.0021
```

CKM Unitarity

Experimental value

 $|Vus| = 0.2200 \pm 0.0026$

 $\Delta |Vus| = 0.0074 \pm 0.0033 \qquad ~2.2 \sigma \text{ discrepancy}$

To solve the problem – measurement with precision ~ 1% (limited by theory) Semileptonic decays $K \rightarrow \pi ev$ best for determination of |Vus| The Ke3 matrix element is parameterized by one form factor

$$M = C \frac{G_F}{\sqrt{2}} V_{us} l^{\mu} f_+^{(o)}(t) (p_K + p_{\pi})_{\mu}$$

Vector current transition matrix element

$$\begin{aligned} f_{+}^{(o)}(t)(p_{K}+p_{\pi})_{\mu} = <\pi |V_{\mu}^{4}-iV_{\mu}^{5}|K> \\ f_{+}^{(o)}(t) = f_{+}^{(o)}(0)[1+\lambda_{+}\frac{t}{m_{\pi^{\pm}}^{2}}] & \lambda_{+} \text{experimentally} \\ \text{measured} \end{aligned}$$

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CKM Unitarity

Recent experimental data – evidence for non linear terms

$$f_{+}^{(o)}(t) = f_{+}^{(o)}(0)[1 + \lambda_{+} \frac{t}{m_{\pi^{\pm}}^{2}} + \lambda_{+}^{'} \frac{t^{2}}{m_{\pi^{\pm}}^{4}}]$$

Experimental data ~ 30 years old Recent measurements - K+e3 (E865, 2003), NA48 and K⁰e3 - (KTeV), NA48,KLOE,prel are significantly above previous results. Accuracy – better then 1%



 $K_{L}^{0} \rightarrow \pi ev$

Experimental result

 $Br(K_{L}^{0} e3)/Br(2tr) = 0.4978 \pm 0.0035$

To determine $Br(K_{L}^{0} \rightarrow \pi ev)$ we need $Br(K_{L}^{0} \rightarrow 3\pi^{0})$ PDG04: $Br(K_{L}^{0} \rightarrow 3\pi^{0}) = 0.2105 \pm 0.0028$ KTeV $Br(K_{L}^{0} \rightarrow 3\pi^{0}) = 0.1945 \pm 0.0018$? Average according PDG prescription $Br(K_{L}^{0} \rightarrow 3\pi^{0}) = 0.1992 \pm 0.0070$

 $Br(K_{L}^{0} e3) = 0.4010 \pm 0.0028_{exp} \pm 0.0035_{norm}$

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Measurement of $Br(K^0_L \rightarrow 3\pi^0)$



In a good agreement with KTeV and KLOE results

Precise measurement of V_{us}

Results for $Br(K^0_L \rightarrow 3\pi^0)$



Measurement of Br(K[±] $\rightarrow \pi^0 e^{\pm} v$)

Preliminary NA48/2 result on Br(K[±] $\rightarrow \pi^0 e^{\pm} v$)

Br(K⁺ $\rightarrow \pi^{0} e^{+} v) = (5.163 \pm 0.021_{stat} \pm 0.056_{syst}) \%$

Br(K⁻ $\rightarrow \pi^{0} e^{-} v) = (5.093 \pm 0.028_{stat} \pm 0.056_{syst}) \%$

 $Br(K^{\pm} \rightarrow \pi^{0} e^{\pm} v) = (5.14 \pm 0.02_{stat} \pm 0.06_{syst}) \%$



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Ke3 form factors



New NA48 results

Determination of V_{us}

The physical quantity

$$\Gamma(\mathbf{K}_{e^{3(\gamma)}}) = \Gamma(\mathbf{K}_{e^{3}}) + \Gamma(\mathbf{K}_{e^{3\gamma}}) + \dots$$

where the radiative corrections with virtual and real photos are taken into account Is well defined, calculable and measurable! The decay density distribution is given by

$$\rho(y, z) = NS_{EW}A(y, z) |f_+(t)|^2$$

where $S_{EW}(M_{\rho,}, M_Z)$ is a short-distance enhancement factor and $y=2E_{\pi}/M_K$, $z=2E_e/M_K$,

$$N = C^2 \frac{G_F^2 |V_{us}|^2 M_K^5}{128\pi^3}$$

Precise measurement of V_{us}

Then

$$\Gamma(K_{e^{3}(\gamma)}) = NS_{EW} | f_{+}^{K\pi}(0) |^{2} I_{K}$$

where I_{K} is the phase-space integral

$$I_{K} = \int_{D} dy dz A(y, z) \frac{|f_{+}(t)|^{2}}{|f_{+}(0)|^{2}}$$

For linear parameterization of $f_{+}(t)$ we have

$$I_{K} = a_0 + a_1 \lambda_+ + a_2 (\lambda_+)^2$$

and for quadratic parameterization of $\boldsymbol{f}_{_{\!\!\!\!+}}(t) \boldsymbol{I}_{\!\!\!\!\!K}$ is given by

$$I_{K} = a_{0} + a_{1}\lambda_{+} + a_{2}(2\lambda_{+} + \lambda_{+}^{2}) + a_{3}\lambda_{+}\lambda_{+} + a_{4}(\lambda_{+})^{2}$$

Precise measurement of V_{us}

|Vus| can be extracted from $K \rightarrow \pi ev$ via

$$|V_{us}| \cdot f_{+}^{K\pi}(0) = \sqrt{\frac{128 \pi^{3} \Gamma(Ke3(\gamma))}{C^{2} G_{F}^{2} M_{K}^{5} S_{EW} I_{K}}}$$

Where:

Sew = 1.0232 – short distance enhancement $\begin{bmatrix} \text{factor}, \\ 1 \\ K_{e^3} \end{bmatrix}$ - phase space integral, $C = \begin{cases} 1 \\ 1 \\ 1/\sqrt{2} \end{cases}$

We followed the prescription for Vus determination proposed in V.Cirigliano, M. Knecht, H. Neufeld, H. Rupertsberger, P. Talavera, In Eur.Phys.J. C23 p121, 2002 V.Cirigliano, H. Neufeld, H. Pichl, Eur.Phys.J. C35 p53, 2004 Important – to treat all experimental data in the same way! Radiative corrections (including virtual and real photons)! A few %

Prescription

- Accept all photon energies
- Accept all angles between pion and positron
- •Accept only pion and positron energies within the original 3-body Dalitz plot.

 Inclusive rate obtained by integrating over the original domain

Experimentally – inclusive measurement of Br(Ke3). For determination of Vus, the corresponding Br(Ke3) should be inside the Dalitz plot. Corrections are: $C_{\rm K}$ =0.58% for K⁰ and $C_{\rm K}$ =0.56% for K⁺



Input for calculation of V_{us}



Experimental data

To have comparable results

Experimental data should be treated in the same way

- -Inclusive measurement of the Br(Ke3)
- -Correct account for radiative corrections, including real photons

Two classes of data on measurement of Br(Ke3) Old data – actually what is included in PDG 2004 New data – published or reported in 2003 and 2004

Old experimental data - K[±]

```
Direct measurement of Br(Ke3)
   dominating experiment Chiang et al., Phys.Rev.D6, 1972, p.1254 accuracy ~ 2%
\succ
    Ke3 measurement is nor inclusive
   No radiative corrections
   The decays \pi \rightarrow \mu are not taken into account
   The Dalitz decays of \pi^0 are not taken into account
                     In the PDG fit also contribute
   Br(Ke3)/Br(2\pi)
\succ
   -in the dominating experiment (~ 5% acc.) rad. corrections without real \gamma
   Br(K_{u3})/Br(K_{e3})
\succ
    K. Horie, Phys. Lett. B513, p. 311, 2001
    The measurement is not inclusive
    Ke3\gamma is considered as background
```

Old experimental data – K⁰

There is no direct measurement of Br(Ke3) In the PDG fit contribute

> $Br(K_{\mu3})/Br(K_{e3}) - 4$ experiments with good statistic

- Two of them are perfect, both measure Br(K_{µ3})/Br(K_{e3}) = 0.662 close to KTeV result
- The other two Hydrogen bubble chambers
 - In this case separation of Ke3 and K μ 3 decays is extremely difficult
 - `50% of the events are ambiguous to separate complicated weighting procedure

Their results shift $Br(K_{\mu3})/Br(K_{e3})$ to 0.697

in strong disagreement with recent measurements

The other contribution is from Kreutz, ZPHY C55, p.67, 1995 – the results from this experiment are in strong contradictions with recent measurements

Experimental data

The careful investigation of old experimental data on measurement of Br(Ke3) leads to the definite conclusion that due to different reasons they are not enough accurate and are not suitable for extraction of Vus matrix element

In what follows we will use only the new high statistics experimental data on measurement of Br(Ke3)

Br(Ke3)



Slope of the $f_{+}(t) - K_{L}^{0}$



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Slope of the $f_+(t) - K^{\pm}$



Mean life time



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Calculation of
$$f_{+}^{K\pi}(0)$$

Quenched lattice calculations – Becirevic at al.

$$\tilde{f}_{+}^{K^{0}\pi^{-}}(0)=0.960\pm0.009$$

$$\tilde{f}_{+}^{K\pi}(0)|_{p^6} = -0.017 \pm 0.008$$

Cirigliano, Neufeld and Pichl

Calculation using χ PT with virtual photons and leptons

- Isospin breaking by the quark masses up to O((m_u-m_d)p²)
- Isospin conserving contribution from SU(3) breaking O(p⁶)
- Electromagnetic effects up to O(e²p²)

$$f_{+}^{K^{0}\pi^{+}}(0) = 0.981 \pm 0.010$$

$$f_{+}^{K^{+}\pi^{0}}(0) = 1.002 \pm 0.010$$

Calculation of $f_{+}^{K\pi}(0)$

To extract Vus we have used the following values

	LO + NLO QCD	EM. radiative corrections	NNLO QCD	total
K ⁰	0.97699±0.00002	0.0046±0.0008	-0.001±0.010	0.981±0.010
K+	1.0002±0.0022	0.0032±0.0016	-0.001±0.010	1.002±0.010
K ⁰	0.97699±0.00002	0.0046±0.0008	-0.017±0.009	0.965±0.009
K+	1.0002±0.0022	0.0032±0.0016	-0.017±0.009	0.986±0.010

The main uncertainty (~1%) comes from O(p⁶) contribution

Determination of V_{us}f₊(0) –NA48

$$|V_{us}| \cdot f_{+}^{K^{0}\pi^{+}}(0) = 0.2146 \pm 0.0016$$

$$|V_{us}| \cdot f_{+}^{K^{+}\pi^{0}}(0) = 0.2250 \pm 0.0013$$

$$|V_{us}| \cdot f_{+}^{K^{-}\pi^{0}}(0) = 0.2235 \pm 0.0014$$

$$|V_{us}| \cdot f_{+}^{K^{+}\pi^{0}}(0) = 0.2245 \pm 0.0013$$

$$|V_{us}| f_{+}(0)$$

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Uncertainty in V_{us} is dominated by the theory!

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Precise measurement of V_{us}

Results – K⁰

Linear approximation of f₊(0)

$$f_{+}^{K^{0}\pi^{+}}(0) = 0.981 \pm 0.010$$

Experiment	Br	$V_{us}f_{+}(0)$	V _{us}
PDG	0.3881±0.0027	0.2116±0.0009	0.2157±0.0024
NA48	0.4020±0.0030	0.2154±0.0009	0.2196±0.0024
KTeV	0.4067±0.0011	0.2166±0.0006	0.2208±0.0023
KLOE – K _L	0.3994±0.0035	0.2147±0.0011	0.2188±0.0025
KLOE – K _S	(7.09±0.11).10 ⁻⁴	0.2165±0.0017	0.2208±0.0022
Average K _L	0.4056±0.0017	0.2164±0.0007	0.2206±0.0024

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Precise measurement of V_{us}

Results – K⁺

Linear approximation of f₊(0)

$$f_{+}^{K^{+}\pi^{0}}(0) = 1.002 \pm 0.010$$

Experiment	Br [%]	$V_{us}f_{+}(0)$	V _{us}
PDG	4.84±0.09	0.2179±0.0020	0.2174±0.0030
NA48	5.14±0.06	0.2245±0.0013	0.2241±0.0026
E865	5.13±0.10	0.2243±0.0022	0.2239±0.0031
Average	5.137±0.051	0.2245±0.0012	0.2240±0.0025



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Precise measurement of V_{us}

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Consistency of K_L and K_{ch} data

Ratio of $f_{+}(0)$ for K_{L} and K^{+} can be measured

$$R = f_{+}^{K^{0}\pi^{+}}(0) / f_{+}^{K^{+}\pi^{0}}(0)$$

Its calculation is free from many of the theoretical uncertainties

$$R^{th} = 1.022 \pm 0.003 - 16\pi \alpha X_1$$

$$1.017 \le R^{th} \le 1.027$$

From the averaged K_L and K^+ data we obtain

 $R^{\text{exp}} = 1.038 \pm 0.006$

In disagreement with theoretical predictions ~ 2σ

- failure of the naïve dimensional analysis for X₁
- failure of chiral power counting
 wrong mean life times

If we use for V_{us} determination

$$f_{+}^{K^{0}\pi^{+}}(0) = 0.965 \pm 0.009 \qquad f_{+}^{K^{+}\pi^{0}}(0) = 0.986 \pm 0.010$$

$$|V_{us}|^{K^0\pi^+} = 0.2242 \pm 0.0022$$

$$|V_{us}|^{K^{\pm}\pi^{0}} = 0.2277 \pm 0.0026$$

The values of V_{us} are changed ~ 2σ Calculation of $f_{+}(0)$ is the most important problem to be solved

Determination of V_{us}



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Non linear approximation leads to

$$\begin{aligned} |V_{us}|.f_{+}^{K^{0}\pi^{+}}(0) = 0.2174 \pm 0.0010 \\ |V_{us}|^{K^{0}\pi^{+}}(0) = 0.2216 \pm 0.0025 \\ |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2248 \pm 0.0026 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2248 \pm 0.0026 \\ |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2248 \pm 0.0026 \\ \end{bmatrix} \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2253 \pm 0.0024 \\ |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.2285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0.285 \pm 0.0027 \\ \end{bmatrix} \\ \begin{bmatrix} |V_{us}|^{K^{\pm}\pi^{0}}(0) = 0$$

Determination of f₊(0)

If we suppose that CKM matrix is unitary

 $|V_{us}| = 0.2274 \pm 0.0021$

then we can determine the values of $f_{+}(0)$ using

$$|V_{us}|.f_{+}^{K^{0}\pi^{+}}(0) = 0.2164 \pm 0.0007$$

$$V_{us} \mid .f_{+}^{K^{\pm}\pi^{0}}(0) = 0.2245 \pm 0.0012$$

$$f_{+}^{K^{0}\pi^{+}}(0) = 0.952 \pm 0.009$$

$$f_{+}^{K^{+}\pi^{0}}(0) = 0.987 \pm 0.010$$

The non linear approximation does not effects the result significantly

$$f_{+}^{K^{0}\pi^{+}}(0) = 0.9561 \pm 0.0086$$

$$f_{+}^{K^{+}\pi^{0}}(0) = 0.991 \pm 0.011$$

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Precise measurement of V_{us}

Conclusions- V_{us}

- The careful analysis of the existing data has shown
 - \succ the old measurements are not suitable for determination of V_{us}
 - > new measurement of all kaon branching fractions is desirable
 - ➢ new more precise measurements of Ke3 and Kµ3 form factors are needed
 - > new measurement of the kaon mean life times will be welcome
 - KLOE and part of NA48 data are still preliminary
- Vus values obtained using average values of Br(Ke3)
 - Support the unitarity of CKM matrix
 - > Strongly depend from the values of $f_+(0)$
 - ➢ More precise calculation of O(p⁶) contribution is required
- The experimental data for R are in disagreement with theoretical predictions
- Measured values of f₊(0) (with unitary CKM matrix) cause questions to the theory